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**Interaction Matrix Selection in Spatial
Econometrics with an Application to
Growth Theory**

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Abstract

The interaction matrix, or spatial weight matrix, is the fundamental tool to model cross-sectional interdependence between observations in spatial econometric models. However, it is most of the time not derived from theory, as it should be ideally, but chosen on an ad hoc basis. In this paper, we propose a modified version of the J test to formally select the interaction matrix. Our methodology is based on the application of the robust against unknown heteroskedasticity GMM estimation method, developed by Lin & Lee (2010). We then implement the testing procedure developed by Hagemann (2012) to overcome the decision problem inherent to non-nested models tests.

An application of the testing procedure is presented for the Schumpeterian growth model with worldwide interactions (Ertur & Koch 2011) using three different types of interaction matrices: genetic distance, linguistic distance and bilateral trade flows. We find that the interaction matrix based on trade flows is the most adequate. Finally, we propose a network based innovative representation of spatial econometric results.

Keywords: Bootstrap; GMM; Interaction matrix; J tests ; Non-nested models; Heteroskedasticity; Spatial autoregressive model

JEL classification: C21- C12 - C52 - O4

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1 Introduction

The interaction matrix, or spatial weight matrix, is the fundamental tool needed to model cross-sectional interdependence between observations in spatial econometric models. It allows to specify the structure of interaction or connectivity within a system through a spatial econometric model and is presumed to be known and exogenous (Anselin & Bera 1998). However, it is most of the time not derived from theory, as it should be ideally, but chosen on an ad hoc basis. In practice, an applied researcher has to choose a priori the interaction matrix, most of the time without any theoretical guidance. As a result, in empirical studies, interaction matrices are generally based on geographical distance, whose exogeneity is widely admitted. Nevertheless, other concepts of similarity or proximity can be useful to explain interactions. Indeed, by analogy to Akerlof (1997), countries or regions can be seen as localized in some general socio-economic, institutional or political space defined by a set of factors. Implementation of spatial econometric models thus requires the proper definition of the similarity or proximity measure to be used for building the interaction matrix.

Moreover, the consequences of a misspecification of the interaction matrix can be severe. For example, Lee (2008) shows that the misspecification of the interaction matrix can cause a significant bias in the estimates of the spatial autoregressive parameter in a SAR model. If the interaction matrix is under-specified, then both the two stage least squares (2SLS) and maximum likelihood (ML) estimator of the spatial autoregressive parameter are biased downward. Inversely, if the interaction matrix is over-specified, the spatial autoregressive parameter is overestimated. Furthermore, the under-specification of the interaction matrix is more problematic than its over-specification in terms of both bias and RMSE.

A special attention should therefore be given to the choice of the interaction matrix since it is given its specific characteristics that spatial econometric models are estimated and cross-sectional interdependence as well as spillovers are evaluated. One of the key points in the specification of spatial econometric models is then the choice, given a criterion, of the most relevant interaction

matrix in a subset of all possible matrices.

As different types of interaction structures can be specified to study the same phenomenon, it can prove to be difficult to identify the most appropriate interaction matrix. The literature on the tests of non-nested models has nevertheless made possible the handling of such situations. The literature devoted to the tests of non-nested assumptions finds its origins in many papers including those of Cox (1961, 1962), Atkinson (1970), Davidson & MacKinnon (1981), Pesaran (1974), Pesaran & Deaton (1978), MacKinnon et al. (1983), Godfrey (1983) and Pesaran & Weeks (2001). The tests of non-nested models are classified in two broad categories. The first one is the test of Cox (1961, 1962), adapted to linear regression models by Pesaran (1974) and to non-linear regression models by Pesaran & Deaton (1978). The second category is due to Davidson & MacKinnon (1981). These authors develop several procedures, closely related to each others, which may be used to test against several alternative models simultaneously.

In the spatial econometrics literature, one can find a first contribution in Anselin (1988). More recently, Kelejian (2008) extended the J test of Davidson & MacKinnon (1981) to a spatial context.¹ The principle of the J test is to estimate a model which contains the null model and the predictive power of alternative models. Then the significance of additional terms is tested. Since this test does not use available information in an efficient way, Kelejian & Piras (2011) and Burridge (2012) suggest different improvements. Kelejian & Piras (2011) modify the way available information is used in determining the predictions and consequently improve the power of the J test. Burridge (2012) advocates the use of parameter estimates obtained from maximum likelihood estimation. Finally in an alternative approach, Jin & Lee (2013) extend the Cox test (Cox 1961, 1962) to a spatial framework. Moreover, in the closely related econometric network literature, an extension of the Kelejian's (2008) J test is proposed by Liu et al. (2014) to differentiate between the local-aggregate and the local-average endogenous peer effects in an econometric network model with network fixed effects.

We propose in this paper a modified version of the J test based on the Robust to unknown

¹Not to be confused with the Hansen-Sargan J test for over-identification in GMM estimation.

heteroskedasticity Generalized Method of Moments (RGMM) estimation method elaborated by Lin & Lee (2010). However it is well known in the literature that all the non-nested hypotheses tests suffer from a decision problem: in some circumstances, they may not help discriminating between the null and alternative models. To overcome this decision problem, Hagemann (2012) recently suggests a simple test for non-nested models, namely the *MJ* test, that we present here in the framework of spatial econometric models.

We finally apply the preceding non-nested hypothesis tests to the generalized Schumpeterian growth model proposed by Ertur & Koch (2011). These authors propose a theoretical and methodological framework taking into account technological interactions between countries to explain the growth process in a Schumpeterian perspective. Worldwide interdependence, implied by international R&D spillovers, are therefore structurally introduced in a growth model with technological interactions, which yields a spatial econometric reduced form. This model includes both factor accumulation and innovation caused by R&D investments as determinants of the growth process, with technological diffusion occurring between interacting pairs of countries, human capital, reflecting the capacity for absorption of technology and physical capital playing the usual part.

In this paper, we consider three different interaction schemes to model the links between countries. The first one is based on genealogical or genetic distance, also called coancestry coefficient Reynolds et al. (1983). This concept of distance, defined by Spolaore & Wacziarg (2009, 2013), based on Cavalli-Sforza et al. (1994), corresponds to the time elapsed since two populations shared a common ancestor.²

In this setting, genealogical distance is considered as a proxy for cultural, institutional and linguistic similarities. The results of Spolaore & Wacziarg (2009) suggest that this general measure of genealogical relatedness between populations can explain cross-country income differences. Their interpretation is that genealogical distance captures the obstacles to the diffusion of development. The second interaction matrix we consider is based on linguistic proximity following Melitz &

²For other empirical works taking into account the ancestral composition of current populations see also Putterman & Weil (2010); Comin et al. (2010); Ashraf & Galor (2013).

Toubal (2014). Melitz & Toubal (2014) summarize the evidence about the linguistic influences in an index, named Common Language Index (CL), resting strictly on exogenous linguistic factors. This summary index (CL) is constructed from different proxies: Common Official Language (COL), Common Native Language (CNL) and Language Proximity (LP). The third interaction matrix used is based on trade flows. Indeed, trade flows may proxy multi-country technological interactions.

The use of the MJ test provides considerable help in the selection of the interaction matrix. Indeed, in the context of this application, we show that the trade flows based interaction matrix is the most appropriate pattern to model interactions between countries, among the three types of interaction patterns we consider. Furthermore, we propose a network based innovative representation of spatial econometric results. The obtained graphs significantly contribute to the interpretation of the estimated model.

The remainder of the paper is organized as follows: in section 2, we present the RGMM estimation approach robust to unknown heteroskedasticity elaborated by Lin & Lee (2010). Section 3 is devoted to model interpretation. Our modified version of the J test based on RGMM estimation as well as the predictor selection are then presented in section 4. The MJ test framework recently developed by Hagemann (2012) is then applied to our specific context of interaction matrix selection in section 5. Section 6 presents the application to the generalized Schumpeterian growth model while section 7 concludes.

2 GMM robust to heteroskedasticity

The model considered in this paper is the heteroskedastic SAR specification

$$Y_n = X_n\beta_0 + \lambda_0 W_n Y_n + \varepsilon_n. \quad (1)$$

where X_n is a $n \times k$ matrix of exogenous and non-stochastic explanatory variables, W_n is a non-stochastic interaction matrix whose diagonal elements are zero, λ_0 is the true parameter measuring

interactions' intensity while β_0 is the true $k \times 1$ vector of unknown parameters associated to the explanatory variables. Finally, ε_n is the vector of independent error terms with ε_{in} characterized by a zero mean and a variance σ_{in}^2 , $i = 1, \dots, n$. We also note $\theta_0 = [\lambda_0, \beta_0']'$ and $\theta = [\lambda, \beta']'$ for any value of λ and β .³ Additionally, $S_n = (I_n - \lambda_0 W_n)$, $S_n(\lambda) = (I_n - \lambda W_n)$ and we define $\varepsilon_n(\theta) = S_n(\lambda)W_n Y_n - X_n \beta$ for any value of θ . Finally, for any square matrix A_n , we define $A_n^s = A_n + A_n'$. This last notation is used in the expressions for identification and asymptotic distribution.

Lin & Lee (2010) show that the (quasi-) maximum likelihood estimator of model (1) is generally inconsistent in presence of unknown heteroskedasticity. Alternative estimation methods are thus required. The Two-Stage Least Squares (2SLS) approach (Kelejian & Prucha 1998), the Best 2SLS (Lee 2003) and the series Best 2SLS (Kelejian et al. 2004) could be considered, but according to Kelejian & Prucha (2010, p.60), the asymptotic normality is not guaranteed under unknown heteroskedasticity. Kelejian & Prucha (2010) generalize the method introduced in Kelejian & Prucha (1999) to estimate a SAR model with SAR disturbances in the presence of unknown heteroskedasticity. They combine a generalized method of moments estimator (GMME) for the coefficient of spatial autocorrelation in the error term to a 2SLSE for the coefficient λ_0 associated to the spatial lag.

In this paper, we apply the approach developed by Lin & Lee (2010) to estimate (1).⁴ The advantage of GMM procedure over 2SLS is that the former remains consistent even if none of the explanatory variable is relevant (Lee 2007). Besides, 2SLS, as will be shown later on, only uses the information contained in the deterministic part of the reduced form of (1), leaving the information in the stochastic part of the reduced form unexploited. Hence, the GMME will be more efficient than the 2SLSE. Lin & Lee (2010) generalize Lee (2007) and Liu et al. (2010) where the focus is on homoskedastic error terms. With that respect, the main differences in the estimation procedure

³In this paper, we note λ_0 and β_0 as the true value of the parameters, $\hat{\lambda}$ and $\hat{\beta}$ as estimators of λ_0 and β_0 and λ and β as parameters on which we maximize the objective function. Hence, only $\hat{\lambda}$ and $\hat{\beta}$ are viewed as random variables.

⁴The estimation procedure developed in Kelejian & Prucha (2010) could also have been used since they use the same moment conditions as Lin & Lee (2010).

due to relaxing the homoskedasticity assumption come from the hypothesis on quadratic moments and the absence of a Best Optimal GMME (BOGMME).

The objective of this section is to present GMM estimation in the presence of unknown heteroskedasticity. The set of assumptions presented below corresponds to those developed in Lin & Lee (2010) and are reproduced for the sake of readability of the paper.

Assumption 1 *The ε_{in} 's are independent $(0, \sigma_{in}^2)$ with finite moments larger than the fourth order such that $\mathbf{E}|\varepsilon_{in}|^{4+\eta}$ for some $\eta > 0$ are uniformly bounded for all n and i .*

As orthogonality conditions require the computation of mean and variances of quadratic forms, one needs to impose the uniform boundedness of moments of order higher than 4.

Assumption 2 *The elements of the $n \times k$ regressors matrix X_n are uniformly bounded constants, X_n has a full rank k and $\lim_{n \rightarrow \infty} \frac{1}{n} X_n' X_n$ exists and is nonsingular.*

Assumption 3 *The interaction matrices W_n and the matrix S_n^{-1} are uniformly bounded in absolute value in both row and column sums.*

Assumption 3 means that the inverse of $S_n = I_n - \lambda_0 W_n$ should be uniformly bounded in absolute value (in addition to W_n). It is important to note that the uniform boundedness is only imposed at the true parameter value and not for any value of λ . Assuming the existence of S_n^{-1} , the reduced form of model (1) is as follows

$$Y_n = S_n^{-1} X_n \beta + S_n^{-1} \varepsilon_n, \quad (2)$$

where $S_n^{-1} = I_n + \lambda_0 W_n + \lambda_0^2 W_n^2 + \dots$.

From (2), we can express $W_n Y_n$ as follows:

$$W_n Y_n = G_n X_n \beta_0 + G_n \varepsilon_n, \quad (3)$$

with $G_n = W_n S_n^{-1}$.

2.1 Orthogonality conditions

In general, $W_n Y_n$ is correlated with ε_n since $\mathbf{E}((W_n Y_n)' \varepsilon_n) = \text{tr}(\Sigma_n G_n) \neq 0$ where Σ_n is a diagonal matrix containing the residual variance $\sigma_{in}^2 = \mathbf{E}(\varepsilon_{in}^2)$ for $i = 1, \dots, n$. The GMM approach developed by Lin & Lee (2010) combines linear moments (identical to 2SLS method) and quadratic moments. Let Q_n be a $n \times k^*$ matrix of IV's, with $k^* \geq k + 1$, which contains the information of the deterministic part $\mathbf{E}(W_n Y_n | X_n)$ of $W_n Y_n$ in (3). This matrix is constructed from X_n and functions of W_n . It can be used to instrument $W_n Y_n$ and X_n . For instance, $Q_n = [X_n, W_n X_n, W_n^2 X_n, \dots]_{LI}$, where LI stands for linearly independent columns.

Lin & Lee (2010) additionally consider quadratic moments $(P_{jn} \varepsilon_n(\theta))' \varepsilon_n(\theta)$ that capture the information contained in the stochastic part of (3). These quadratic moments serve as IV's for $G_n \varepsilon_n$, the non-deterministic part of $W_n Y_n$. One needs to impose some conditions on P_{jn} matrices so that quadratic moments can act as orthogonality conditions ($\mathbf{E}[\varepsilon_n' P_{jn}' \varepsilon_n] = 0$), i.e. $P_{jn} \varepsilon_n$ is uncorrelated with ε_n . Let $\mathcal{P}_{1n}$ be the class of constant $n \times n$ matrices with zero trace. Consider a subclass $\mathcal{P}_{2n}$ of $\mathcal{P}_{1n}$ that contains constant $n \times n$ matrices with zero diagonal. Depending on the assumptions made on the error term, matrices P_{jn} may belong to $\mathcal{P}_{1n}$ or $\mathcal{P}_{2n}$.

Let us consider heteroskedastic error terms with, as variance-covariance matrix, the diagonal matrix Σ_n , made of σ_{in}^2 , the individual variances. The orthogonality condition associated to a given matrix P_{jn} is $\mathbf{E}(\varepsilon_n' P_{jn}' \varepsilon_n) = \text{tr}(\Sigma_n P_{jn})$. The only way for this trace to be 0 is that $P_{jn} \in \mathcal{P}_{2n}$. The intuition is that when P_{jn} has zero diagonal, the l^{th} element of $P_{jn} \varepsilon_n = \sum_{k=1}^n p_{lk,jn} \varepsilon_{kn}$ excludes the corresponding element of ε_n (ε_{ln}) from the sum since $p_{ll,jn} = 0$. So, each component of $P_{jn} \varepsilon_n$ is uncorrelated with the corresponding component of ε_n . Imposing homoskedasticity of the error term, $\mathbf{E}(\varepsilon_n' P_{jn}' \varepsilon_n) = \sigma_0^2 \text{tr}(P_{jn})$. Hence, P_{jn} is only required to have a zero trace for this expression to be null (Lee 2001, 2007).

However, no matter the hypothesis on the variance of the error term, we need $P_{jn} \varepsilon_n$ to be correlated with $W_n(I_n - \lambda_0 W_n)^{-1}$ for $P_{jn} \varepsilon_n$ to act as an instrument for $G_n \varepsilon_n$ and the closest P_{jn} is of $W_n(I_n - \lambda_0 W_n)^{-1}$, the better the instrument.

Quadratic moments are used for 2 reasons. As they capture the information contained in the stochastic part of (3), they make the obtained estimator more efficient compared to 2SLS or B2SLS estimators. Second, if all X_n are irrelevant, linear moments can not be used to instrument $W_n Y_n$. However, in that case, which corresponds to the pure SAR model, i.e. $Y_n = \lambda W_n Y_n + \varepsilon_n$, quadratic moments can still act as instruments for $W_n Y_n$.

Assumption 4 *The matrices $P_{n,j}$'s whose diagonal elements are 0 ($P_{n,j} \in \mathcal{P}_{n2}$) are uniformly bounded in both row and column sums, and elements of Q_n are uniformly bounded.*

Under heteroskedasticity, the set of moment functions, assuming m quadratic moments, is:

$$\begin{aligned} g_n(\theta) &= (P_{1n}\varepsilon_n(\theta), \dots, P_{mn}\varepsilon_n(\theta), Q_n)' \varepsilon_n(\theta) \\ &= (\varepsilon_n(\theta)' P_{1n}\varepsilon_n(\theta), \dots, \varepsilon_n(\theta)' P_{mn}\varepsilon_n(\theta), \varepsilon_n(\theta)' Q_n)' \end{aligned} \quad (4)$$

2.2 Asymptotic properties

Assumption 5 ensures the identification of θ_0 from the orthogonality conditions $E(g_n(\theta_0)) = 0$, for a sufficiently large n .

Assumption 5 *Either:*

- a) $\lim_{n \rightarrow \infty} \frac{1}{n} Q_n' (G_n X_n \beta_0, X_n)$ has the full rank $k + 1$, or
- b) $\lim_{n \rightarrow \infty} \frac{1}{n} Q_n' X_n$ has the full rank k , $\lim_{n \rightarrow \infty} \frac{1}{n} \text{tr}(\Sigma_n G_n^s P_{jn}) \neq 0$ for some j and $\lim_{n \rightarrow \infty} \frac{1}{n} (\text{tr}(\Sigma_n G_n' P_{1n} G_n), \dots, \text{tr}(\Sigma_n G_n' P_{mn} G_n))'$ are linearly independent.

Assumption 6 focuses on the parameter space for θ .

Assumption 6 θ_0 is in the interior of the parameter space Θ , which is a bounded subset of $\mathcal{R}^{k+1}$.

By contrast to maximum likelihood estimation, λ is not required to belong to some compact

parameter space.⁵ The constraints imposed on the parameter space ensure the positiveness of the Jacobian of the transformation $|I_n - \lambda W_n|$. However, in the GMM framework, such constraints are not relevant because the objective function is a polynomial function (of order 4) in θ . The condition on the boundedness of the parameter space is solely for the theoretical purpose of proving consistency of the GMME (Lin & Lee 2010). Hence, the GMM is a unconstrained estimation procedure.

Instead of minimizing the objective function $g_n(\theta)'g_n(\theta)$ with respect to θ , Lin & Lee (2010) propose to minimize a linear combination $a_n g_n(\theta)$ of the moment functions $g_n(\theta)$, so that the objective function enters the Hansen (1982) setting where each condition is weighted by its precision. The matrix a_n has a full rank greater than or equal to the dimension of θ . The objective function is thus $g_n(\theta)'a_n' a_n g_n(\theta)$ where the matrix $a_n' a_n$ is non-negative and contains the weight of each orthogonality condition and motivates the issue of optimal weighting.

To express the asymptotic distribution of the Robust (to the presence of unknown heteroskedasticity) GMME, we need the expression of the gradient of $g_n(\theta_0)$ as well as the variance matrix of the orthogonality conditions (also evaluated at the true parameters values):

$$D_n = \frac{\partial \mathbf{E}(g_n(\theta_0))}{\partial \theta'} = - \begin{pmatrix} \text{tr}(\Sigma_n P_{1n}^s G_n) & 0 \\ \vdots & \vdots \\ \text{tr}(\Sigma_n P_{mn}^s G_n) & 0 \\ Q_n' G_n X_n \beta_0 & Q_n' X_n \end{pmatrix} \quad (5)$$

$$\Omega_n = \text{Var}(g_n(\theta_0)) = \begin{pmatrix} \text{tr}(\Sigma_n P_{n,1}(\Sigma_n P_{1n})^s) & \text{tr}(\Sigma_n P_{1n}(\Sigma_n P_{2n})^s) & \cdots & 0 \\ \text{tr}(\Sigma_n P_{n,2}(\Sigma_n P_{1n})^s) & \text{tr}(\Sigma_n P_{2n}(\Sigma_n P_{2n})^s) & \cdots & 0 \\ \vdots & \vdots & & \vdots \\ 0 & 0 & \cdots & Q_n' \Sigma_n Q_n \end{pmatrix} \quad (6)$$

Lin & Lee (2010) show that under Assumptions 1-6, and that $\lim_{n \rightarrow \infty} \frac{1}{n} a_n D_n$ exists and has the

⁵For more information about the parameter space for λ , the interested reader may consult Kelejian & Prucha (2010).

full rank $k + 1$, the Robust GMME $\widehat{\theta}$ is a consistent estimator of θ_0 and $\sqrt{n}(\widehat{\theta} - \theta_0) \xrightarrow{D} N(0, \Gamma)$, where

$$\Gamma = \lim_{n \rightarrow \infty} \left(\frac{1}{n} D_n' a_n' a_n D_n \right)^{-1} D_n' a_n' a_n \Omega_n a_n' a_n D_n (D_n' a_n' a_n D_n)^{-1} \quad (7)$$

2.3 Optimal RGMME

Even though the choice of the weighting matrix $a_n' a_n$ does not affect the consistency of RGMME, it plays a role in its efficiency. By setting $a_n' a_n$ equal to the inverse of the covariance matrix of orthogonality conditions (Ω_n), one obtains the optimal RGMME, i.e. the most efficient estimator given $g_n(\theta)$. In their proposition 3, Lin & Lee (2010) show that if one has a consistent estimator $\widehat{\Omega}_n$, the asymptotic distribution of the feasible “optimal” RGMME obtained from minimizing $g_n(\theta)' \widehat{\Omega}_n g_n(\theta)$ with respect to θ is as follows:

$$\sqrt{n}(\widehat{\theta} - \theta_0) \xrightarrow{D} N \left(0, \left(\lim_{n \rightarrow \infty} \frac{1}{n} D_n' \widehat{\Omega}_n^{-1} D_n \right)^{-1} \right) \quad (8)$$

The optimal estimator is the most efficient estimator that can be obtained given a set of orthogonality conditions. However, we could question the existence of the best choice of orthogonality conditions, i.e. the set of conditions which guarantees that the best optimal RGMME is the most efficient one. Unfortunately, in the unknown heteroskedasticity case, no such set of orthogonality conditions exists, since they would involve the unknown Σ_n . However, Lin & Lee (2010) suggest to use as orthogonality conditions those corresponding to the best conditions in the *iid* case when $P_{jn} \in \mathcal{P}_{n,2}$. These conditions, shown in Lee (2007), are $P_n = (G_n - \text{Diag}(G_n))$ and $Q_n = [G_n X_n \beta_0, X_n]$, where $\text{Diag}(A_n)$ refers to a diagonal matrix where diagonal elements correspond to the diagonal of A_n .⁶ Hence, they suggest to use only one quadratic and $k + 1$ linear conditions. The vector of orthogonality conditions becomes:

$$g_n(\theta) = (\varepsilon_n'(\theta) P_n \varepsilon_n(\theta), \varepsilon_n' Q_n)' \quad (9)$$

⁶If quadratic moments P_n belong to $\mathcal{P}_{n,1}$, Liu et al. (2010) derive the best moment conditions under homoskedasticity, no matter the distribution of the error terms.

Expressions for the gradient and the covariance matrix of $g_n(\theta)$ defined in (9), evaluated at the true parameter value are:

$$D_n = -\frac{\partial \mathbf{E}(g_n(\theta_0))}{\partial(\theta)} = \begin{pmatrix} \text{tr}(P_n^s G_n \Sigma_n) & 0 \\ Q_n' G_n X_n \beta_0 & Q_n' X_n \end{pmatrix} \quad (10)$$

$$\Omega_n = \text{Var}(g_n(\theta_0)) = \begin{pmatrix} \text{tr}(\Sigma_n P_n (\Sigma_n P_n)^s) & 0 \\ 0 & Q_n' \Sigma_n Q_n \end{pmatrix} \quad (11)$$

As these orthogonality conditions depend on the unknown parameters λ_0 and β_0 , we need to proceed in 2 steps to get the optimal RGMME. The first stage consists in getting consistent estimators of λ_0 and β_0 . To do so, we compute RGMME based on orthogonality conditions not involving any unknown parameters but which satisfy the above assumptions. For instance, we set $P_n = W_n$ and $Q_n = [X_n, W_n X_n, W_n^2 X_n]$. Also we use as initial guess of the weight matrix $a_n' a_n$ the identity matrix. The obtained (first-step) estimators, $\check{\lambda}^{fs}$ and $\check{\beta}^{fs}$, are then used to compute the residuals which allow to have an estimator $\check{\Sigma}_n$, whose i^{th} diagonal element is $\check{\varepsilon}_{in}^2(\check{\theta})$. We are now able to compute an estimator $\check{\Omega}_n$ of Ω_n . Besides, we can construct the new orthogonality conditions $g_n^{st} = (\varepsilon_n'(\theta) P_n^{st} \varepsilon_n(\theta), \varepsilon_n'(\theta) Q_n^{st})'$ based on $P_n^{st} = (\check{G}_n - \text{Diag}(\check{G}_n))$ and $Q_n^{st} = [\check{G}_n X_n \check{\beta}^{fs}, X_n]$, where $\check{G}_n = W_n(I_n - \check{\lambda}^{fs} W_n)^{-1}$.

The second steps consists in minimizing the objective function shown in (12) with respect to θ :

$$g_n^{st}(\theta)' \check{\Omega}_n^{-1} g_n^{st}(\theta) \quad (12)$$

Statistical inference will be based on this second step estimator $\hat{\theta}$, which has an estimated asymptotic covariance matrix equal to $\left(\frac{1}{n} \hat{D}_n' \hat{\Omega}_n^{-1} \hat{D}_n\right)^{-1}$. In this expression, $\hat{D}_n$ is constructed from plugging the second step estimators within equation (10) and $\hat{\Omega}_n$ comes from plugging the second step estimators in equation (11).

3 Interpretation of the SAR model

Let us now consider the interpretation of the estimation results of the heteroskedastic SAR model in terms of the impact of a variation of an independent variable on the dependent variable. As the model is estimated in implicit form (1), we need to rely on its reduced form to provide economic interpretations. The reduced form in (2) can be explicitly written as follows:

$$Y_n = \sum_{h=1}^k \beta_{0,h} (I_n - \lambda_0 W_n)^{-1} X_{n,h} + (I_n - \lambda_0 W_n)^{-1} \varepsilon_n \quad (13)$$

Taking the first order partial derivatives of Y_n with respect to $X_{n,h}$, for $h = 1, \dots, k$, we then obtain, the so-called $(n \times n)$ impact matrices, one for each of the k explanatory variables:

$$\Xi_n^{(h)} = \frac{\partial Y_n}{\partial X_{n,h}'} = \beta_{0,h} (I_n - \lambda_0 W_n)^{-1} = \beta_{0,h} \sum_{v=0}^{\infty} \lambda_0^v W_n^v = \beta_{0,h} (I_n + \lambda_0 W_n + \lambda_0^2 W_n^2 + \lambda_0^3 W_n^3 + \dots) \quad (14)$$

where $(I_n - \lambda_0 W_n)^{-1}$ is the so-called *global interaction multiplier*.⁷ Note that the impact matrices are generally full and not symmetric regardless of the sparsity and structure of the interaction matrix W_n . We call the country in column j of this matrix the emitting country and country in row i the receiving country.

For the explanatory variable X_h , the diagonal elements of the impact matrix, specified in equation (14), which we call the direct impacts, are heterogeneous in presence of spatial autocorrelation due to higher order feedback effects. More precisely, the own derivative for country i includes feedback effects where country i affects country j and country j also affects country i as well as longer paths which might go from country i to j to k and back to i . This is what Debarsy & Ertur (2010) call *interactive heterogeneity*, by contrast to standard individual heterogeneity in panel data

⁷To empirically compute expression (14), we have to replace the true values of the parameters by their estimated counterparts.

models.⁸

$$Diag(\Xi_n^{(h)}) = \beta_{0,h}I_n + \beta_{0,h}Diag(\lambda_0^2W_n^2 + \lambda_0^3W_n^3 + \dots) \quad (15)$$

The magnitude of those direct effects mostly depends on the value of $\beta_{0,h}$, which is constant across the sample. Heterogeneity thus comes from the second term on the right hand side of equation (15) representing the magnitude of pure feedback effects, which depends again on $\beta_{0,h}$, on the values of powers of λ_0 , and on the interconnection structure of the observations embedded in the powers of the interaction matrix W_n . It is nevertheless likely to be negligible compared to the value of $t\beta_{0,h}$ in most of applied works.

However the main question in this type of spatial econometric specification concerns the impact of a variation of an explanatory variable in a country i on the dependent variable in other countries of the sample, which we call the indirect effects, i.e. the off-diagonal terms of the impact matrix, and which represent the *spillovers*. They are presented in expression (16):

$$\Xi_n^{(h)} - Diag(\Xi_n^{(h)}) = \beta_{0,h}\lambda_0W_n + \beta_{0,h}[\lambda_0^2W_n^2 - Diag(\lambda_0^2W_n^2)] + \beta_{0,h}[\lambda_0^3W_n^3 - Diag(\lambda_0^3W_n^3)] + \dots \quad (16)$$

By contrast to direct effects, the main part is played here by the informational content and the structure of the interaction matrix W_n , which is the main source of heterogeneity, parameters λ_0 and $\beta_{0,h}$ being constant across the whole sample. Again, high order terms in the infinite sum in (16) may be negligible compared to the values of W_n . Not surprisingly, strongly connected countries are more impacted than less connected countries. However, spillovers diffuse to the entire sample.

Finally, the sum of the i^{th} row of the impact matrix (14) represents the total impact on the dependent variable in country i due to a 1 unit change in $X_{n,h}$ in each of the countries in the sample. The sum of column j gives the total impact on the dependent variable of all the countries of a 1 unit change of $X_{n,h}$ in country j , which is of particular interest in terms of interpretation

⁸We call those effect directs impacts since we compute the impact of the variation of an explanatory variable in country i , the emitting country on itself.

here.

4 The modified J test based on RGMM

For ease of exposition, let us consider that under the null hypothesis H_0 and the $M - 1$ alternative hypotheses $H_{1,m}, m = 2, \dots, M$, we have heteroskedastic SAR models which only differ by the specification of the interaction matrix.

$$H_0 : Y_n = X_n\beta_1 + \lambda_1 W_{1n}Y_n + \varepsilon_{1n}, \quad (17)$$

$$H_{1,m} : Y_n = X_n\beta_m + \lambda_m W_{mn}Y_n + \varepsilon_{mn}, \quad (18)$$

The general motivation of the J test is to estimate a model which contains the null model and the predictive power of alternative models in order to check if predictors from alternative models can significantly contribute to the explanatory power in the null model. For the homoskedastic case, different predictors have been derived by Kelejian & Prucha (2007) which are presented here for the sake of comparison with the heteroskedastic case. The first predictor $\hat{y}_{in|1}^m$ is obtained from the reduced form of the alternative model m :

$$\begin{aligned} \hat{y}_{in|1}^m &= \mathbf{E}(y_{in}|\Lambda_1) \\ &= (I_n - \lambda_m W_{mn})_{i.}^{-1} X_n \beta_m, \end{aligned} \quad (19)$$

where $A_{i.}$ means the i^{th} row of matrix A . This predictor is based on the smallest information set, namely $\Lambda_1 = \{X, W_{mn}\}$. The second predictor is based on a larger information set, namely $\Lambda_2 = \{X, W_{mn}, W_{mn,i}Y_n\}$. It is obtained from the structural form of the alternative model m and

is computed as follows:

$$\begin{aligned}\widehat{y}_{in|2}^m &= \mathbf{E}(y_{in}|\Lambda_2) \\ &= \lambda_m W_{mn,i} Y_n + X_{i,n} \beta_m + \frac{\text{cov}(\varepsilon_{in}, W_{mn,i} Y_n)}{\text{var}(W_{mn,i} Y_n)} [W_{mn,i} Y_n - \mathbf{E}(W_{mn,i} Y_n)]\end{aligned}\quad (20)$$

where $W_{mn,i}$ is the i^{th} row of W_{mn} . Also, the last term takes into account the correlation between the error term and the spatial lag of the dependent variable. The different elements involved in this correlation are computed as follows:

$$\begin{aligned}\mathbf{E}(W_{mn,i} Y_n) &= W_{mn,i} (I - \lambda_m W_{mn})^{-1} X_n \beta_m \\ \Sigma_m^y &= (I - \lambda_m W_{mn})^{-1} (I - \lambda_m W_{mn}')^{-1} \\ \text{var}(W_{mn,i} Y_n) &= \sigma_n^2 W_{mn,i} \Sigma_m^y W_{mn,i}' \\ \text{cov}(\varepsilon_{in}, W_{mn,i} Y_n) &= \sigma_n^2 (I - \lambda_m W_{mn}')^{-1} X_n \beta_m\end{aligned}\quad (21)$$

where σ_n^2 is the variance of the error term in the homoskedastic case. Since the second information set is larger than the first one, the second predictor is more efficient (Kelejian & Prucha 2007). A third predictor is sometimes considered due to its intuitive appeal. It is also based on the information set Λ_2 but assumes a zero correlation between the error term and the spatial lag of the dependent variable:

$$\widehat{y}_{in|3}^m = \lambda_m W_{mn,i} Y_n + X_{i,n} \beta_m.$$

Kelejian & Prucha (2007) show that it is biased since the spatial lag is assumed independent of the error term. We will thus do not consider it.⁹

Let us now study the predictors in the heteroskedastic case. Theoretically, we can use the first two predictors above. The first one, $\widehat{y}_{in|1}^m$, is not affected by the presence of heteroskedasticity and takes the same expression as for homoskedastic errors (equation 19). However, for the second predictor, $\widehat{y}_{in|2}^m$, the variance of the spatial lag and the covariance between the spatial lag and the

⁹Finally, Kelejian & Prucha (2007) propose the full information predictor but it is not more efficient than the second for the SAR specification.

error term have to be adapted for heteroskedasticity. They are presented in expression (22),

$$\begin{aligned} \text{var}(W_{mn,i}Y_n) &= \sigma_{i,mn}^2 W_{m,i} \Sigma_m^y W'_{mn,i} \\ \text{cov}(\varepsilon_{in}, W_{mn,i}Y_n) &= \sigma_{i,mn}^2 (I - \lambda_m W'_{mn})^{-1} X_n \beta_m \end{aligned} \quad (22)$$

where $\sigma_{i,mn}^2$ is the variance of the error term of individual i in model m . The drawback of this predictor is that it involves the terms $\sigma_{i,mn}^2$ which are evaluated by computing $\hat{\varepsilon}_{i,mn}^2$ but cannot be consistently estimated. However, even though Λ_1 is smaller than Λ_2 , we show in section 4.2 below, using Monte Carlo experiments, that the first predictor should be preferred over the second to construct the J test. In the following, we will thus only consider the first predictor for the sake of clarity.¹⁰

Let us denote $\hat{Y}_n^M = [\hat{y}_n^2, \dots, \hat{y}_n^M]$, the $n \times (M - 1)$ matrix containing the $M - 1$ predicted alternative models using the first predictor. We then augment the model under the null (model 17) with the predictors $\hat{Y}_n^M$:

$$Y_n = X_{1n}\beta_1 + \lambda_1 W_{1n}Y_n + \hat{Y}_n^M \delta + \varepsilon_{1n}, \quad (23)$$

where δ is a $(M - 1) \times 1$ vector of parameters: $\delta' = [\delta_2, \dots, \delta_M]$. If the model under the null is the correct model, then: δ should not significantly differ from 0. This is the J test.

Our J test procedure based on the RGMM estimation procedure is summarized in the following steps:

Step 1: Estimate the parameters β_m and λ_m for $m = 2, \dots, M$ by the two-step optimal RGMM approach described in section 2.

Step 2: Estimate $\hat{y}_n^m$ for $m = 2, \dots, M$ and form $\hat{Y}_n^M = [\hat{y}_n^2, \dots, \hat{y}_n^M]$.

Step 3: Estimate the augmented model $Y_n = X_{1n}\beta_1 + \lambda_1 W_{1n}Y_n + \hat{Y}_n^M \delta + \varepsilon_{1n}$ by the two-step optimal RGMM approach described in section 2.

¹⁰The computation of the J test and the MJ test are not affected by using the second predictor.

Note that the predicted values do not add any difficulties to the model and are simply included in the set of exogenous variables : $\tilde{X} = [X, \hat{Y}_n^M]$ (see Davidson & MacKinnon 1981, p.785).

Step 4: Construct the J test

Define $\gamma_1 = (\beta'_1, \lambda_1, \delta')'$. Let $R = (0_{(M-1) \times (k_1+1)}, I_{(M-1)})$ so that $R\gamma_1 = 0$. Then, the J statistic defined as a Wald statistic is:

$$J_{1,n} = (R\hat{\gamma}_1)' \left[R(\hat{D}'_n(\hat{\Omega}_n^{-1})\hat{D}_n)^{-1}R' \right]^{-1} (R\hat{\gamma}_1) \sim \chi^2(M-1). \quad (24)$$

where $\hat{D}'_n$ and $\hat{\Omega}_n^{-1}$ are respectively the gradient and the inverse of the covariance matrix of the augmented two-step RGMM estimation procedure. In this paper, we follow Davidson & Mackinnon (1985) who suggest to use the variance-covariance of the augmented specification.¹¹

4.1 Statistical inference based on bootstrap

Davidson & MacKinnon (2002) show that statistical inference based on asymptotic theory causes size distortion of the J test while a bootstrap approach performs better in small sample sizes. Burrige & Fingleton (2010) implement a semi-parametric bootstrap approach to the J test applied to the choice of the interaction matrix in spatial econometrics.¹² They show that statistical inference based on bootstrap outperforms statistical inference based on asymptotic distribution for the J statistic. Besides, Jin & Lee (2015) formally prove the consistency of the bootstrap approach in spatial econometrics for linear-quadratic forms of residuals test-statistics, such as Moran's I or J test. In this paper, to account for heteroskedasticity, we follow Hagemann (2012) and implement the wild bootstrap of Liu (1988) and Mammen (1992). It consists in perturbing the residuals

¹¹Alternatively, Davidson & Mackinnon (1985) also suggest to use the estimated covariance matrix coming from the estimation of the model under the null hypothesis. However, the Monte Carlo simulations we performed indicate poor performance of this alternative method.

¹²Burrige & Fingleton (2010) consider a homoskedastic error term, a first step estimation procedure based on maximum likelihood and an augmented model estimated by IV. We differ from that paper by allowing unknown heteroskedasticity in the error term and estimating all models by Robust GMM.

with *iid* copies $\eta_1, \eta_2, \dots, \eta_n$ of a random variable η with $\mathbf{E}(\eta|y, \mathcal{F}) = 0$, $\mathbf{E}(\eta^2|y, \mathcal{F}) = 1$ and $\mathbf{E}(|\eta|^{2+\zeta}|y, \mathcal{F}) < \infty$ for some $\zeta > 0$. Hagemann (2012), following Davidson & Flachaire (2008), recommends the use of a Rademacher distribution for η that takes on the value 1 with probability 0.5 and -1 with probability 0.5. Finally, let H be a diagonal matrix having as diagonal elements the terms $\eta_1, \eta_2, \dots, \eta_n$.

Consider model (17) as the model under the null

- i*) Compute the J test associated to this model using the methodology presented above and label it $\widehat{J}_{1,n}$.
- ii*) Estimate model (17) to get $\widehat{\beta}_1$, $\widehat{\lambda}_1$ and the residuals $\widehat{\varepsilon}_{1n}$
- iii*) Generate $\varepsilon_{1n}^* = H\widehat{\varepsilon}_{1n}$
- iv*) Generate the bootstrapped sample $Y_n^* = (I_n - \widehat{\lambda}_1 W_{1n})^{-1}[X_n \widehat{\beta}_1 + \varepsilon_{1n}^*]$
- v*) Compute the bootstrapped J test for the model (17) using the bootstrapped dependent variable Y_n^* and label it $J_{1,n}^*$.

Repeat operations *ii*) to *v*) B times, each with a new realization of H . Reject the null hypothesis at the α threshold if $\widehat{J}_{1,n}$ is larger than $c_{1-\alpha}^*$, the $1 - \alpha$ empirical quantile of the distribution of $J_{1,n}^*$.

4.2 Monte Carlo experiments

In this section, we perform Monte Carlo experiments to compare the small sample properties of the J test using the first or the second predictor. Theoretically, even though the information set for the second predictor (based on the structural form) is larger than for the first predictor (based on the reduced form), we have seen that the former requires the estimation of σ_i^2 for which no consistent estimator exists. The objective of these Monte Carlo experiments is to assess the importance of this drawback in small samples.

We consider the following DGP:

$$Y_n = \lambda W_n Y_n + \beta_0 \iota_n + X_{1n} \beta_1 + X_{2n} \beta_2 + \varepsilon_n. \quad (25)$$

where ι_n is the unit vector, $X_{1n} \sim U(0, 10)$, $X_{2n} \sim N(0, 1)$ and the associated vector of parameters β_0 , β_1 and β_2 are all set equal to 1. In these simulations, the regressors are kept constants across replications. The error term is assumed heteroskedastic and non-normally distributed. More precisely, it is designed in the following way:

$$\varepsilon_{in} = \bar{\sigma} \left(\frac{\nu_{in} - 2}{\sqrt{2}} \right) X_{i,1n}, \quad (26)$$

where ν_{in} follows a $\Gamma(2, 1)$ distribution. Besides, to make simulation results comparable across different values of parameters, we set the average dispersion of the error term ($\bar{\sigma}$) so that the signal to noise ratio is equal to 0.6. This signal to noise ratio is computed as the ratio of the explained variance over the total variance, ignoring spatial autocorrelation (see Lee 2007, Liu et al. 2010). This ratio would correspond to a goodness of fit of 0.6 in a standard regression.

The spatial autoregressive parameter λ varies from 0.2 to 0.8 by increment of 0.2 to capture low, moderate and high spatial autocorrelation. Two sample sizes, $n = 100$ and $n = 254$, are considered, corresponding respectively to the number of counties in North Carolina and in Texas. We use different interaction matrices W_n to cover sparse and dense interaction schemes. Definition of the W_n considered is given in Table 1. Finally, for each case, we perform 1000 replications.

Table 1: Definition of the interaction matrices

Name	Expression
Inverse exponential distance	$w_{ij} = e^{-d_{ij}}$
Inverse square distance	$w_{ij} = 1/d_{ij}^2$
5 <i>nn.</i>	$w_{ij} = \begin{cases} 1 & \text{if } j \text{ is in the 5 } nn. \text{ of } i \\ 0 & \text{otherwise} \end{cases}$
20 <i>nn.</i>	$w_{ij} = \begin{cases} 1 & \text{if } j \text{ is in the 20 } nn. \text{ of } i \\ 0 & \text{otherwise} \end{cases}$

Note: The distance between 2 observations is computed as the geodesic distance and *nn.* stands for nearest neighbors.

Tables 2 and 3 compare the performance in terms of rejection rate of the J test when constructed

Table 2: Comparison of J test performance for the 2 predictors, $n = 100$

λ	First Predictor				Second Predictor			
	Rej. Rate J test M1		Rej. Rate J test M2		Rej. Rate J test M1		Rej. Rate J test M2	
	Boot.	Asymp.	Boot.	Asymp.	Boot.	Asymp.	Boot.	Asymp.
	A) M1: $W = 5$ nearest neighbors ; M2: $W = 20$ nearest neighbors							
0.2	0.047	0.048	0.416	0.443	0.069	0.328	0.116	0.401
0.4	0.045	0.050	0.916	0.941	0.057	0.260	0.521	0.884
0.6	0.049	0.055	0.995	0.996	0.050	0.232	0.923	0.993
0.8	0.050	0.065	0.989	0.996	0.052	0.311	0.998	0.999
	B) M1: $W = 5$ nearest neighbors ; M2: $W =$ Exponential inverse distance							
0.2	0.039	0.054	0.513	0.558	0.055	0.399	0.138	0.442
0.4	0.040	0.050	0.973	0.981	0.049	0.238	0.662	0.944
0.6	0.040	0.048	1.000	1.000	0.038	0.099	0.975	0.998
0.8	0.040	0.049	1.000	1.000	0.043	0.054	0.999	1.000
	C) M1: $W = 5$ nearest neighbors ; M2: $W =$ Inverse square distance							
0.2	0.049	0.019	0.538	0.565	0.050	0.202	0.135	0.406
0.4	0.049	0.019	0.972	0.983	0.038	0.263	0.698	0.937
0.6	0.048	0.026	1.000	1.000	0.044	0.358	0.985	0.999
0.8	0.052	0.037	1.000	1.000	0.042	0.281	0.999	1.000
	D) M1: $W = 20$ nearest neighbors ; M2: $W = 5$ nearest neighbors							
0.2	0.054	0.074	0.225	0.251	0.062	0.341	0.024	0.295
0.4	0.049	0.068	0.676	0.697	0.046	0.316	0.058	0.394
0.6	0.046	0.069	0.940	0.943	0.040	0.366	0.333	0.678
0.8	0.045	0.066	0.997	0.997	0.047	0.420	0.777	0.934
	E) M1: $W = 20$ nearest neighbors ; M2: $W =$ Exponential inverse distance							
0.2	0.039	0.061	0.281	0.291	0.072	0.419	0.023	0.319
0.4	0.038	0.062	0.778	0.787	0.058	0.257	0.101	0.476
0.6	0.036	0.055	0.976	0.977	0.032	0.102	0.502	0.837
0.8	0.037	0.057	1.000	1.000	0.055	0.093	0.919	0.987
	F) M1: $W = 20$ nearest neighbors ; M2: $W =$ Inverse square distance							
0.2	0.043	0.026	0.272	0.292	0.075	0.237	0.015	0.236
0.4	0.043	0.032	0.743	0.757	0.045	0.150	0.14	0.426
0.6	0.049	0.039	0.962	0.964	0.045	0.148	0.567	0.820
0.8	0.044	0.039	0.999	1.000	0.043	0.130	0.948	0.988
	G) M1: $W =$ Exponential inverse distance ; M2: $W = 5$ nearest neighbors							
0.2	0.045	0.062	0.119	0.134	0.078	0.355	0.020	0.285
0.4	0.044	0.061	0.361	0.401	0.060	0.344	0.027	0.172
0.6	0.044	0.057	0.806	0.857	0.059	0.289	0.428	0.618
0.8	0.049	0.061	0.999	1.000	0.050	0.369	0.968	0.985
	H) M1: $W =$ Exponential inverse distance ; M2: $W = 20$ nearest neighbors							
0.2	0.038	0.049	0.114	0.141	0.074	0.428	0.020	0.282
0.4	0.041	0.046	0.340	0.402	0.056	0.356	0.022	0.152
0.6	0.040	0.048	0.804	0.852	0.042	0.327	0.410	0.601
0.8	0.044	0.053	0.999	1.000	0.117	0.633	0.971	0.987

Table 3: Comparison of J test performance for the 2 predictors, $n = 254$

λ	First Predictor				Second Predictor			
	Rej. Rate J test M1		Rej. Rate J test M2		Rej. Rate J test M1		Rej. Rate J test M2	
	Boot.	Asymp.	Boot.	Asymp.	Boot.	Asymp.	Boot.	Asymp.
	A) M1: $W = 5$ nearest neighbors ; M2: $W = 20$ nearest neighbors							
0.2	0.046	0.045	0.969	0.974	0.056	0.231	0.321	0.665
0.4	0.048	0.045	1.000	1.000	0.039	0.173	0.939	1.000
0.6	0.045	0.044	0.998	0.998	0.036	0.237	0.998	1.000
0.8	0.048	0.066	0.999	0.999	0.055	0.371	1.000	1.000
	B) M1: $W = 5$ nearest neighbors ; M2: $W =$ Exponential inverse distance							
0.2	0.040	0.049	0.984	0.986	0.059	0.118	0.498	0.745
0.4	0.041	0.049	1.000	1.000	0.047	0.069	0.995	1.000
0.6	0.042	0.051	1.000	1.000	0.045	0.055	1.000	1.000
0.8	0.046	0.055	1.000	1.000	0.049	0.057	1.000	1.000
	C) M1: $W = 5$ nearest neighbors ; M2: $W =$ Inverse square distance							
0.2	0.046	0.053	0.99	0.99	0.038	0.105	0.525	0.741
0.4	0.048	0.050	1.000	1.000	0.033	0.165	0.999	1.000
0.6	0.047	0.054	1.000	1.000	0.039	0.22	1.000	1.000
0.8	0.048	0.054	1.000	1.000	0.047	0.168	1.000	1.000
	D) M1: $W = 20$ nearest neighbors ; M2: $W = 5$ nearest neighbors							
0.2	0.065	0.071	0.552	0.569	0.062	0.283	0.050	0.258
0.4	0.061	0.072	0.975	0.977	0.026	0.294	0.331	0.582
0.6	0.056	0.068	0.999	1.000	0.027	0.494	0.804	0.928
0.8	0.056	0.080	0.999	0.999	0.034	0.561	0.986	0.997
	E) M1: $W = 20$ nearest neighbors ; M2: $W =$ Exponential inverse distance							
0.2	0.050	0.056	0.670	0.683	0.059	0.119	0.064	0.288
0.4	0.050	0.055	0.988	0.990	0.051	0.076	0.421	0.711
0.6	0.046	0.064	1.000	1.000	0.046	0.068	0.873	0.976
0.8	0.046	0.062	0.999	0.999	0.046	0.071	0.997	1.000
	F) M1: $W = 20$ nearest neighbors ; M2: $W =$ Inverse square distance							
0.2	0.044	0.057	0.693	0.702	0.067	0.127	0.093	0.236
0.4	0.045	0.053	0.995	0.995	0.039	0.111	0.514	0.742
0.6	0.045	0.054	1.000	1.000	0.042	0.161	0.934	0.985
0.8	0.050	0.054	1.000	1.000	0.039	0.141	0.999	1.000
	G) M1: $W =$ Exponential inverse distance ; M2: $W = 5$ nearest neighbors							
0.2	0.061	0.066	0.441	0.462	0.083	0.295	0.140	0.215
0.4	0.062	0.067	0.990	0.992	0.046	0.248	0.925	0.947
0.6	0.065	0.071	1.000	1.000	0.057	0.479	1.000	1.000
0.8	0.065	0.062	1.000	1.000	0.123	0.527	1.000	1.000
	H) M1: $W =$ Exponential inverse distance ; M2: $W = 20$ nearest neighbors							
0.2	0.052	0.053	0.453	0.475	0.076	0.276	0.135	0.217
0.4	0.055	0.054	0.992	0.993	0.041	0.278	0.916	0.948
0.6	0.051	0.057	1.000	1.000	0.108	0.698	1.000	1.000
0.8	0.061	0.064	1.000	1.000	0.032	0.064	1.000	1.000

from the first or the second predictor for each of the two sample sizes: 100 and 254. In these Monte Carlo, we consider two competing SAR models which only differ by the interaction matrix. The first model (M1) is the true model while the second model (M2) is based on a wrong interaction matrix. Hence, the rejection rate of the J statistic associated to M1 assesses the size of the test while the rejection rate of the J test of M2 is a measure of its power. In the simulations we also compare the performance of the test based on an asymptotic distribution (χ_1^2) with the performance based on bootstrap, where 399 replications were used.

We first analyze the results of Table 2, associated to $n = 100$. For both predictors, the size of the test based on bootstrap is always around the theoretical value of 5% which shows the good performance of the bootstrap approach. However, when considering asymptotic distribution, size distortion appears, especially for the second predictor, with rejection rates reaching 42%, instead of the theoretical 5%. For the bootstrap inference, we thus cannot base our predictor selection on size considerations. Looking at rejection rates of the J test associated to M2, we observe important difference between the 2 predictors, no matter the interaction matrices used in the 2 models. The rejection rate for the first predictor is much higher than for the second one, implying a higher power. This is especially true for low to moderate values of λ but differences are also noticeable for higher values of λ . We also note a lower power for the second predictor when inference is based on bootstrap rather than on asymptotic distribution while it is not the case for the first predictor.

The same patterns are observed considering the bigger sample size, $n = 254$, as shown in Table 3. Power differences between the 2 predictors are still present, even though less important. This result may be explained by the increase in the number of observations. Nevertheless, we also observe cases where the second predictor performs poorly compared to the first predictor. For instance, in case D) , when $\lambda = 0.4$ the bootstrapped power for Predictor 2 is equal to 0.331 while for Predictor 1, we observe a bootstrapped power of 0.975.

Hence, mainly for power reasons, we propose to rely on the first predictor (based on the reduced form of the alternative model) to construct the J test.

5 The MJ -test

The J test presented above is a procedure for testing a null model against non-nested alternatives. It is generally known that tests of non-nested models may cause to a problem of model selection when inverting the null and alternative hypotheses do not give clear-cut results. To overcome this drawback, Hagemann (2012) suggests a simple test, the MJ (minimum J) statistic which allows to always select a model between competing alternatives. The MJ statistic consists in selecting the model with the smallest associated J statistic value. In this paper, we extend the use of the MJ test procedure to a spatial framework and more precisely to the selection of the interaction matrix in spatial autoregressive models.

Assume that one wishes to find the most appropriate interaction matrix among a set of M spatial autoregressive models.

$$Y_n = X_n\beta_m + \lambda_m W_{mn}Y_n + \varepsilon_{mn}, \quad m \in \mathcal{M} = \{1, \dots, M\}, \quad (27)$$

with ε_{mn} , the $n \times 1$ vector of independent error terms with $\varepsilon_{i,mn}$ characterized by a zero mean and a variance $\sigma_{i,mn}^2$, $i = 1, \dots, n$ and $\theta_m = (\lambda_m, \beta'_m)'$ is the vector of regression parameters to be estimated for $m = 1, \dots, M$. The MJ test procedure is the following:

Step 1: For each $m \in \mathcal{M}$, compute the J test of the null hypothesis H_0 corresponding to model m against $M - 1$ alternatives non-nested hypotheses.

For this, it is necessary to estimate the augmented model:

$$Y_n = X_{mn}\beta_m + \lambda_m W_{mn}Y_n + \sum_{l \in \mathcal{M} \setminus \{m\}} \delta_l \widehat{y}_n^l + \varepsilon_{mn}. \quad (28)$$

Construct then $\widehat{J}_{m,n}$, the J -test associated to model m , as a test of joint significance of $\delta_l, l \in \mathcal{M} \setminus \{m\}$. The augmented model can be estimated by the two-step optimal RGMM estimation method discussed above.

Step 2: Let $\mathcal{J}_n = \{\hat{J}_{m,n} : m \in \mathcal{M}\}$ and define the least J statistic: $MJ_n = \min \mathcal{J}_n$. This step solves the decision problem inherent to the J test since the preferred model in the set of the M considered specifications will be the one with the smallest value of $\hat{J}_{m,n}$, $m = 1, \dots, M$.¹³

6 Application to the generalized Schumpeterian growth model

The purpose of this section is to apply our testing procedure to the multi-country Schumpeterian growth model with worldwide interactions, proposed by Ertur & Koch (2011). These authors propose an integrated theoretical and methodological framework characterized by technological interactions to explain growth processes from a Schumpeterian perspective. Their generalized Schumpeterian multi-country growth model, extending the one elaborated by Howitt (2000), explicitly takes into account global technological interdependence implied by R&D spillovers. Moreover they show that a multi-country Solow growth model with technological interdependence similar to that proposed by Ertur & Koch (2007) is actually nested in the generalized model leading to a simple test. Therefore, their generalized model can be interpreted as a Schumpeterian extension of the Solow growth model since in addition to factor accumulation, they show that innovation caused by R&D investment plays a major role in explaining the growth process. The model includes both determinants, with technological diffusion occurring concretely between pairs of countries, human capital reflecting absorptive capacity along the lines of Nelson & Phelps (1966), and physical capital playing the usual role. More specifically, they show that when the R&D expenditures have no effect on the growth rate of technology, the multi-country Schumpeterian growth model reduces to the multi-country Solow growth model.¹⁴

Their empirical results show that the multi-country pure Solow growth model is rejected in favor

¹³Hagemann (2012) also proposes to test whether the correct model is part of the considered ones by performing statistical inference on the MJ_n . However, this theoretical consideration can only be assessed in Monte Carlo simulations where the DGP is fixed. The interested reader may consult their Monte Carlo results to obtain further details on the behavior of this test.

¹⁴The interested reader can refer to Ertur & Koch (2011) for the full development of the multi-country Schumpeterian growth model.

of the multi-country Schumpeterian growth model, once both models are integrated in a unified theoretical and methodological framework characterized by technological interdependence. They finally estimate the TFP equation implied by their multi-country Schumpeterian growth model as well as the international R&D spillovers implied by technological interdependence using two different interaction matrices based on geographical distance and trade flows. The main result they underline is the fact that their model allows to have multiple local technological leaders: besides USA, Germany and Japan are also playing that role in their respective area of influence.

6.1 The econometric specification

Due to space limitation, we will focus here more specifically on the TFP equation implied by the multi-country growth model developed by Ertur & Koch (2011, eq. 59, p.234):

$$\ln TFP_i = \beta_0 + \beta_1 \ln \frac{s_{K,i}}{n_i + 0.05} + \beta_2 \ln s_{A,i} + \beta_3 \ln n_i + \gamma H_i \sum_{j \neq i}^n v_{ij} \ln TFP_j + \varepsilon_i \quad (29)$$

where $\ln TFP_i$ is the logarithm of Total Factor Productivity of country i at steady state (taking one third as the capital's share in income); β_1 is the coefficients associated with the logarithm of the investment rate divided by the effective depreciation rate $\ln \frac{s_{K,i}}{n_i + 0.05}$, β_2 is the coefficient associated with the logarithm of the investment rate in the research sector $\ln s_{A,i}$ and β_3 is the coefficient associated to the logarithm of the working-age population growth rate n_i . H_i is the stock of human capital, which is designed to measure the capacity of absorption of new technology for country i . Finally γ is the autoregressive interaction parameter. In matrix form, the model is written as follows, in cross-section:

$$Y = \beta_0 \iota + \beta_1 S_K + \beta_2 S_A + \beta_3 N + \gamma W y + \varepsilon \quad (30)$$

where Y is the $(n \times 1)$ vector of the logarithms of TFP ; ι is the unit vector, S_K is the vector of the logarithms of the investment rates in physical capital divided by the effective depreciation

rates, S_A is the vector of the logarithms of expenditures in the research sector and N is the vector of the logarithms of working-age population growth rates. W is the interaction matrix modeling technological interactions as a function of the new technology absorption capacity of the receiving country and some ad hoc measure of similarity between countries with general term $w_{ij} = H_i v_{ij}$. We will consider in the application different definitions of similarity v_{ij} and select the most relevant one given the information contained in the sample.

6.2 Data and interaction matrices

For the sake of comparability we use the same database as Ertur & Koch (2011). The data are extracted from the Heston et al. (2006) Penn World Tables (PWT version 6.2), containing information on real income, investment and population for a large number of countries. Data on R&D expenditures come from the World Investment Report (2005) of the United Nations Conference on Trade and Development (UNCTD). The sample contains 58 countries and includes 21 OECD countries over the period 1990-2003.¹⁵ The explanatory variables are constructed as follows. To measure n_i , for $i = 1, \dots, n$, as the average growth of the working-age population (ages 15 to 64), it is necessary to compute the number of workers as: $RGDPCH \times POP/RGDPW$, where $RGDPCH$ is real GDP per capita computed by the chain method, $RGDPW$ is real-chain GDP per worker, and POP is the total population. The saving rate $s_{K,i}$, for $i = 1, \dots, n$, is measured as the average share of gross investment in GDP over the period as in Mankiw et al. (1992). The variable $s_{A,i}$, is measured as the average share gross domestic expenditure on R&D (GERD) relative to GDP over the 1991-2001 period. As suggested by Mankiw et al. (1992) among others, we use $g_w + \delta = 0.05$. Finally, the human capital stock is measured using the Mincerian equation, as proposed by Hall & Jones (1999) or Caselli (2005), from the data of the database developed by Cohen & Soto (2007).¹⁶ The dependent variable is defined in Ertur & Koch (p.234,

¹⁵Due to missing data for the computation of the linguistic interaction matrix, we exclude South Korea from the sample as Korean is generally admitted to be a language isolate.

¹⁶This database is available at:
<http://www.parisschoolofeconomics.eu/fr/cohen-daniel/base-de-donnees-internationale-education/>.

2011) and computed as $\ln TFP_i = \ln y_i - 0.5 \ln \frac{s_{K,i}}{n_i + 0.05}$ where y_i is the real income per worker in 2003. Table 4 provides some descriptive statistics over the variables used in our specification.

Table 4: Descriptive statistics					
	Min	Max	Mean	Median	St. err.
$\ln TFP$	3.2444	4.5469	4.1123	4.1789	0.3223
H_i	1.0287	3.4632	2.3597	2.2724	0.6172
$\ln s_A$	-3.6815	-1.3694	-2.5357	-2.6789	0.6779
$\ln n$	-1.5016	-1.3463	-1.4333	-1.4397	0.0427
$\ln \frac{s_K}{n+0.05}$	-0.1363	0.3867	0.2169	0.2284	0.1229

The first interaction matrix $W1$ we consider is based on genealogical or "genetic" distance following Spolaore & Wacziarg (2009, 2013).¹⁷ This notion of distance corresponds to the time elapsed since two populations shared a common ancestor. In other words, the genetic distance is a measure of relatedness between populations over time. It can be interpreted as a general metric for average differences in characteristics transmitted across generations. Moreover they argue that: "...by its very definition, genetic distance is an excellent *summary statistic* capturing divergence in the whole set of implicit beliefs, customs, habits, biases, conventions, etc. that are transmitted across generations - biologically and/or culturally - with high persistence." (Spolaore & Wacziarg 2009, p.471). The general idea is that more closely related societies are more likely to learn from each other and adopt each other's innovations. Spolaore & Wacziarg (2009, 2013) show that this general genealogical measure between populations may then explain income differences today. Their interpretation is that the genetic distance captures the barriers to the diffusion of development.

Several measures of genetic distance have been proposed in the literature related to population genetics. The most popular are FST distance or "co-ancestor coefficient" (Wright 1965) and Nei's distance (Nei 1973). These two measures have slightly different theoretical properties but their correlation is very strong. Thus, the choice of one these should not affect the results. The basic unit of these measures is the allele, which is a form taken by a gene. Differences in allele frequencies

¹⁷The term genetic distance comes from the literature related to population genetics and is also used in linguistics to refer to a measure of relatedness.

hence form the basis of summary measures of calculating distance between populations. The genetic distance matrix $W1$ used here is based on the differentiation coefficient G_{ST} of Nei which corresponds to the probability that two randomly selected variants in a population are different. Nei (1973) propose indexes based on allele frequencies that describe the level and organization of diversity within populations. These indexes portray the total diversity (h_T), the average intra-population diversity (h_S) or differentiation between populations (G_{ST}). G_{ST} takes a value equal to zero if and only if the distributions of alleles are identical between the two populations, whereas it is positive when the distributions of alleles are different. A greater distance measure G_{ST}^W reflects a longer separation between populations. However, like many countries, such as United States and Australia, are composed of sub-populations that are genealogically distant, it is preferable to use a weighted measure of genealogical distance G_{ST} . Thus, the interaction matrix $W1$ is based on a decreasing function of the weighted genealogical distance G_{ST}^W between countries whose functional form is the negative exponential of the distance. The general term of this matrix $W1$ is defined as $w1_{ij} = H_i v1_{ij}$ with:

$$v1_{ij} = \begin{cases} 0 & \text{if } i = j \\ e^{-g_{ij}} / \sum_{j \neq i} e^{-g_{ij}} & \text{otherwise} \end{cases} \quad (31)$$

where g_{ij} represents the weighted genetic distance G_{ST}^W between countries i and j and H_i is the human capital stock of the receiving country i .

The second interaction matrix $W2$ we consider is based on a linguistic proximity concept following Melitz & Toubal (2014). They summarize the evidence about the linguistic influences in an aggregate index, named Common Language index (CL), resting strictly on exogenous linguistic factors. This summary index (CL) is obtained using three indexes: Common Official Language (COL), Common Native Language (CNL) and Language Proximity (LP).¹⁸ The Common Language index (CL) ranges between 0 and 1. More precisely, CL takes a value equal to zero if the degree

¹⁸Data on Common Language are available at http://www.cepii.fr/cepii/en/bdd_modele/presentation.asp?id=19.

of linguistic proximity between two countries is null, whereas CL tends to 1 when the linguistic proximity between these two countries is high. The general term of this matrix $W2$ is defined as $w2_{ij} = H_i v2_{ij}$ with:

$$v2_{ij} = \begin{cases} 0 & \text{if } i = j \\ CL_{ij} / \sum_{j \neq i} CL_{ij} & \text{otherwise} \end{cases} \quad (32)$$

where CL_{ij} represents the Common Language Index (CL) between countries i and j and H_i is the human capital stock of the receiving country i .

The last considered interaction matrix $W3$ is based on trade flows. Indeed, trade flows may proxy multi-country technological interactions.¹⁹ The general term of this matrix is defined as $w3_{ij} = H_i v3_{ij}$ where:

$$v3_{ij} = \begin{cases} 0 & \text{if } i = j \\ m_{ij} / \sum_{j \neq i} m_{ij} & \text{otherwise} \end{cases} \quad (33)$$

where m_{ij} is defined as the average imports of country i coming from country j computed over the 1990-2000 period to prevent endogeneity problems that might arise, using the bilateral trade flows database from CEPIL, and H_i is the human capital stock of the receiving country i . Ertur & Koch (2011) use a different international trade database and define a block triangular interaction matrix assuming that the North club (OECD countries) diffuses its knowledge to the South club (the rest of the countries of their sample), but the opposite does not occur (see Appendix 2, p.250, Ertur & Koch (2011)). Here we relax this assumption and further allow the South club to diffuse its knowledge to the North club. Hence this interaction matrix is full.

¹⁹The choice of this matrix is justified by studies of Grossman & Helpman (1991), Coe & Helpman (1995) and Coe et al. (1997) which show that international trade may be seen as a major diffusion vector of technological progress.

6.3 Econometric results

The TFP equation (29) implied by the multi-country Schumpeterian growth model and the international R&D spillovers implied by technological interdependence, is estimated by the RGMM procedure described in section 2 using the three interaction matrices based on genealogical distance ($W1$), linguistic distance ($W2$), and trade flows ($W3$). Each matrix has been normalized by the minimum between the maximal values of the row sums and column sums, as suggested in Kelejian & Prucha (2010, Lemma 2, p.56). Estimation results are presented in Table 5. They are consistent with those obtained by Ertur & Koch (2011) using different interaction matrices, underlying the robustness of the model.²⁰ The coefficient associated with R&D expenditures is significant whatever the interaction matrix considered. Its estimated value ranges from 0.170 to 0.184. We also note that the spatial autocorrelation parameter is significant and has an estimated value ranging from 0.210 to 0.220. Thus, the TFP of one country cannot be considered as independent from that of other countries. The coefficients of the investment rate divided by the effective depreciation rate and of the working-age population growth rate are non-significant as in Ertur & Koch (2011, Table 2, p.242).

6.3.1 Application of tests for non-nested spatial models

In order to provide considerable help in the selection of the interaction matrix, we apply the J tests to equation (29) and then use the MJ procedure to select the most adequate interaction matrix (amongst those considered). The results are presented in Table 6. We first observe that bootstrapped p-values are much higher than p-values based on asymptotic distribution (χ^2_2). This result is in line with what we found in the Monte Carlo experiments. Further, none of the three J tests are significant, implying a decision problem with respect to the selection of the interaction matrix. Indeed, the (bootstrapped) p-values are all higher than 5%. To overcome this decision

²⁰Note that Ertur & Koch (2011) estimate also a constrained model where they introduce some structural theoretical restrictions $\beta_1 = \beta_2 = \beta_3 = \beta$ (p.241), which would take a lot of space to explain here. Therefore due to space limitation and for more simplicity, we only estimate here the unconstrained model. The interested reader could refer to this paper. Note also that the non-significance of β_1 and β_3 is a shared feature between the two papers.

Table 5: Estimation Results

Estimation method	SAR-RGMM		
Interaction matrix	(W1)	(W2)	(W3)
Constant	4.3673 (3.0078)	4.5860 (3.2079)	4.4174 (3.0574)
$\ln(s_K/(n + 0.05))$	-0.0371 (-0.0966)	-0.0187 (-0.0480)	-0.0648 (-0.1624)
$\ln s_A$	0.1702 (2.2574)	0.1837 (2.4286)	0.1785 (2.3586)
$\ln n$	0.3083 (0.3229)	0.4338 (0.4602)	0.3204 (0.3363)
γ	0.2199 (3.1267)	0.2147 (3.1373)	0.2101 (3.0787)
n	58	58	58
Pseudo- R^2	0.6346	0.6249	0.6257

t-stats between brackets. Pseudo- R^2 is the squared correlation between predicted and actual values.

problem, we use the MJ test and select the model for which the associated J statistic has the minimum value. This minimum value is obtained for the model with $W3$, namely the interaction matrix based on a function of the capacity to absorb new technologies (measured by the stock of human capital of the receiving country) and on trade flows.

Table 6: MJ tests

H_0 :	W1	W2	W3
H_A :	W2,W3	W1,W3	W1,W2
J-test	3.538 (0.354) [0.171]	3.225 (0.383) [0.199]	2.835 (0.512) [0.242]

Bootstrapped p-values between brackets, using 999 replications and asymptotically-based p-values between square brackets.

On the basis of econometric results in Tables 5 and 6 and equation (14), we compute the impacts of home and foreign R&D expenditures on the TFP of a given country using $W3$, which is favored by the MJ test. We then obtain the $n \times n$ estimated matrix of elasticities, using the

estimated coefficients of the econometric model. Results for OECD countries plus Brazil and China, displaying significant impacts are presented in Table 7.²¹

Table 7 is divided in two parts: the upper part displays R&D spillovers within the club of OECD countries (North-North R&D spillovers) while the lower part shows R&D spillovers from OECD countries to countries not belonging to this club (North-South R&D spillovers). Results for China and Brazil are added in the last columns to give an insight into R&D spillovers from non OECD emerging countries to countries belonging to the North club (South-North R&D spillovers) and to the South club (South-South R&D spillovers). The highlighted array elements on the main diagonal correspond to the direct elasticities, including feedback effects, that is the elasticity of the TFP of a given country with respect to its own R&D expenditures.

We first note that the direct elasticities are all significant and only slightly higher than $\hat{\beta}_2 = 0.17855$ when we take into account spatial autocorrelation, because of higher order feedback effects in the expansion (15). Even though these direct effects are heterogeneous by nature, in this application we do not observe much difference between countries, due to the fact that feedback effect are of small scale compared to the estimated value of $\hat{\beta}_2$. It is however interesting to note that those feedback effects are the highest for USA, Germany, Japan, Canada, France and United Kingdom (Figure 1). For OECD countries, they range from 0.1786% for Greece or Portugal to 0.1810% for USA, which benefits of the highest feedback effects, while the average direct impact including feedback effects is 0.1791, i.e. on average, a 1% increase of their R&D expenditures yields a 0.1791% increase of TFP. For countries not belonging to this club, on average, a 1% increase of their R&D expenditures yields a 0.1786% increase in TFP, comparable to the direct impacts for Greece or Portugal.

Figure 2 presents results for significant indirect impacts, for the whole sample, which are our main concern here. Using Table 7, the flow of knowledge between countries i and j goes from the country in column j , the emitting country, to the country in row i , the receiving country. A

²¹Inference on impacts is based on simulating 1000 values of these impacts. As the estimators are shown to be normally distributed, for these simulations, we use a normal distribution centered on the estimated values of the parameters and with the covariance matrix of the estimated parameters.

Figure 1: Direct impacts including heterogeneous feedback effects of a change of R&D expenditures on the TFP of all countries using the trade based interaction matrix ($W3$).

network representation of those significant impacts is also proposed in Figure 3, in terms of weighted out-degrees based on the estimated value of significant indirect elasticities, i.e. the impact on the TFP of country i of a 1% change of R&D expenditures in country j , using the Fruchterman and Reingold force-directed algorithm (see Fruchterman & Reingold 1991).

Second, with respect to indirect elasticities, i.e. the off-diagonal terms of the matrix in Table 7, we note that the United States is the country, among OECD countries, which diffuses the most of its R&D to other countries, followed first by Germany and Japan and second by France, United-Kingdom and Italy (Figures 2 and 3). The indirect impact of a 1% increase of R&D expenditures in USA on the TFP of all other countries is 0.3051%, whereas this impact is 0.2145% for Germany, 0.1718% for Japan, 0.1173% for France, 0.1004 % for Italy and 0.1002% for United Kingdom (see sums of the corresponding columns of Table 7 and Figure 2). Among the OECD group, countries which diffuse the least of their R&D are Greece, New-Zealand and Portugal. Note also that the share of total intra OECD impact in the total impact ranges from 58% for USA to 99% for Portugal. For non-OECD countries, it is interesting to note that for China for instance the indirect impact of a 1% increase of R&D expenditures on the TFP of all other countries is 0.045%, an impact that

Figure 2: Indirect impacts of a change of R&D expenditures on the TFP of all countries using the trade based interaction matrix ($W3$)

is higher than impacts reported for most of the OECD countries. This is also the case for Brazil (0.0478%).

In addition, a 1% increase in R&D expenditures in USA yields a 0.0248% increase in Canadian TFP, whereas a 1% increase in R&D expenditures in Canada only yields a 0.0075% increase in US TFP. This asymmetric effect is mainly due to the asymmetric nature of trade between USA and Canada. On average, for the period under study, only 19.82% of the total imports of USA come from Canada, whereas 67.27% of the total imports of Canada come from USA. Note also that the capacity of absorption of new technologies, as measured by human capital stocks, is slightly higher in USA (3.41) than in Canada (3.29). Figure 4 displays this capacity of absorption for all countries in the sample. Even though the value and significance of estimated coefficients in Table 5 are robust to the choice of interaction matrix, it is nevertheless highly important to select the right interaction matrix. To make our point, we show in Figures 5 and 6 the significant indirect effects obtained for the 2 other considered interaction matrices. We note that their patterns are completely different from each other, implying different policy recommendations. Further, the three local technological leaders identified using the interaction matrix based on trade do not appear anymore for interaction

Figure 3: Network representation of significant indirect impacts (weighted out-degrees).

matrices based on linguistic or genealogical similarity.

It is also possible to interpret the results in terms of clubs. Inside the North club (OECD countries), the average indirect impact is 0.033, i.e. on average, a 1% increase of the R&D expenditures

Figure 4: Human capital stock (h_i) measured using the Mincerian equation, as proposed by Hall & Jones (1999) or Caselli (2005), from the data of the database developed by Cohen & Soto (2007).

Figure 5: Indirect impacts of a change of R&D expenditures on the TFP of all countries using the linguistic distance based interaction matrix (W_2).

Figure 6: Indirect impacts of a change of R&D expenditures on the TFP of all countries using the genealogical distance based interaction matrix ($W1$).

of a OECD country yields a 0.033% increase of the TFP of all other OECD countries. Inside the South club (non-OECD countries), on average, a 1% increase of the R&D expenditures yields a much lower 0.0061% increase of the TFP of the other countries. Not surprisingly, the North-South average indirect impact is on average 0.104%, much higher than the South-North average indirect impact, which is 0.002% (see Table 7). Again, not surprisingly this North-South club heterogeneity comes from indirect effects, the direct effects being pretty similar across clubs.

Third, those results are essentially due to the weight of the United States in the international trade pattern. The United States R&D diffusion impacts are higher for countries belonging to Central and South-America, such as Canada, Mexico, Trinidad and Tobago, Jamaica, Costa-Rica and Honduras for instance than for other countries belonging to the South Club.²² We also note the role played by the human capital stock in enhancing the absorption capacity of international R&D diffusion since the impact on Canada (0.0248%) is higher than the impact on Mexico (0.0186%) although the latter has an higher import share from the United States. These results for United States show the influence of this country in the American continent, as also underlined by Coe et al.

²²In our sample, Canada imports almost 67% from the United States, Mexico, 77%; Trinidad and Tobago, 51%; Jamaica, 54%; Honduras, 56% and Costa-Rica, 53%.

Table 7: Average significant impacts for Clubs

Club	Mean	Median
North - North		
Direct impact	0.1791	0.1788
Indirect impact	0.0331	0.0159
Total impact	0.2121	0.1948
North - South		
Indirect impact	0.1048	0.1048
South - South		
Direct impact	0.1786	0.1786
Indirect impact	0.0061	0.0024
Total impact	0.18543	0.17987
South - North		
Indirect impact	0.0021	0.0003

(1997). The elasticities from Japan to South East Asian countries are also higher than the elasticities from Japan to other countries belonging to the South club. The elasticities from Germany to other European countries are higher than the elasticity from Germany to other countries belonging to the south club. These results suggest that the United States is a natural technological leader for Central and Southern American countries, that Japan is the technological leader in South East Asia and that Germany is the technological leader in Europe.

Finally, using the network representation in Figure 7, obtained by using additional information on the coordinates of the country capitals for the localization of the nodes, we note that knowledge diffuses *locally* between European countries where indirect estimated elasticities are higher for larger emitting countries as Germany, France, United Kingdom or Italy than for smaller countries. confirming that Germany appears as the European technological leader. We also note that the elasticities between European and African countries are relatively high, showing the importance of European countries (essentially France and to some extend United Kingdom) as technological leaders for African countries (see Table 7).²³

²³In Figures 3 and 7, for the sake of readability, we omit of the network representations the links that were very close to 0 (<0.0005).

Figure 7: Network representation of significant indirect impacts (weighted out-degrees). (Nodes are localized using the coordinates of the capitals of the countries of the sample)

7 Conclusions

We propose a solution to the interaction matrix selection problem in spatial econometric models using the RGMM estimation method proposed by Lin & Lee (2010), which consists in a new, robust against unknown heteroskedasticity, version of the J test first proposed by Kelejian (2008) and modified by Kelejian & Piras (2011). Moreover the common model selection problem that arises with non-nested hypotheses tests is overcome using the approach recently proposed by Hagemann (2012), called the MJ test.

We then apply this non-nested hypotheses testing procedure to the the multi-country Schumpeterian growth model proposed by Ertur & Koch (2011) to discriminate between three different types of interaction matrices: genetic distance, linguistic proximity and bilateral trade flows. The estimation results of the TFP equation implied by this model are robust with respect to the choice of the interaction matrix. However using the J test to select an interaction matrix leads to a model selection problem. To overcome this problem, we use the MJ test which indicates that the interaction matrix based on a function of the capacity of absorption of new technologies and trade flows is the most appropriate amongst the three interaction matrices we consider.

The obtained estimation results are consistent with those of Ertur & Koch (2011) and Coe et al. (1997) and highlight the heterogeneity of the international diffusion of knowledge. As already noted by Ertur & Koch (2011), this empirical evidence cannot be captured by the standard Howitt & Aghion (1998) and Howitt (2000) models, which assume that USA are the unique *global* technological leader, whereas the integrated multi-country Schumpeterian growth model allows the emergence of *local* technological leaders. Using the selected trade flows based interaction matrix, we show that indeed USA, but also Germany and Japan actually play the role of *local local* technological leaders.

We believe that the suggested interaction matrix selection procedure will be helpful for applied researchers.

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Table 7: Matrix of significant elasticities at 5% for OECD countries using trade flows ($W3$)

	AUS	AUT	BEL	CAN	DNK	FIN	FRA	GER	GRC	IRL	ITA	JPN
AUS	0.1787	0.0003	-	-	0.0003	0.0004	0.0017	0.0039	0.0001	0.0005	0.0018	0.0090
AUT	-	0.1788	0.0014	-	0.0004	0.0004	0.0025	0.0165	0.0001	-	0.0036	0.0017
BEL	-	-	0.1790	-	0.0003	0.0003	0.0057	0.0081	0.0001	0.0007	0.0021	0.0015
CAN	0.0003	-	-	0.1796	-	-	0.0012	-	-	-	0.0010	0.0042
DNK	-	0.0006	0.0018	-	0.1787	0.0013	0.0029	0.0095	0.0001	0.0005	0.0022	0.0017
FIN	0.0002	0.0006	0.0015	-	0.0013	0.1787	0.0024	0.0076	0.0001	0.0005	0.0021	0.0030
FRA	-	0.0005	0.0033	-	0.0004	0.0004	0.1792	0.0079	0.0001	0.0006	0.0041	0.0019
GER	-	0.0021	0.0033	-	0.0009	0.0006	0.0054	0.1801	0.0002	0.0008	0.0044	0.0032
GRC	-	0.0005	0.0015	-	0.0005	0.0004	0.0033	0.0063	0.1786	0.0004	0.0056	0.0019
IRL	-	-	0.0009	-	0.0004	0.0003	0.0020	0.0032	-	0.1787	0.0012	0.0025
ITA	0.0001	0.0010	0.0020	-	0.0004	0.0003	0.0049	0.0079	0.0002	0.0004	0.1790	-
JPN	0.0011	0.0003	-	0.0016	0.0004	0.0002	0.0015	0.0033	-	0.0005	0.0014	0.1798
NLD	-	0.0005	0.0045	-	0.0005	0.0005	0.0032	0.0092	0.0001	0.0007	0.0019	0.0024
NZL	0.0083	-	-	-	0.0003	0.0003	0.0013	0.0027	-	-	0.0013	0.0072
NOR	-	0.0005	0.0013	0.0011	0.0029	0.0016	0.0022	0.0064	0.0001	0.0006	0.0019	0.0027
PRT	-	0.0003	0.0011	-	0.0002	0.0002	0.0032	0.0044	0.0000	0.0002	0.0025	0.0010
ESP	-	0.0005	0.0015	-	0.0003	0.0003	0.0059	0.0060	0.0001	0.0004	0.0035	0.0015
SWE	-	0.0006	0.0018	-	0.0026	0.0025	0.0030	0.0086	0.0001	0.0006	0.0019	0.0021
CHE	0.0002	0.0019	0.0019	-	0.0005	0.0004	0.0051	0.0146	0.0001	0.0007	0.0047	0.0021
GBR	0.0003	0.0004	0.0023	0.0009	0.0007	0.0006	0.0043	0.0071	0.0001	0.0018	0.0026	0.0030
USA	0.0003	-	-	0.0075	0.0002	0.0002	0.0016	0.0034	0.0000	0.0005	0.0015	0.0089
ARG	0.0001	-	0.0006	-	0.0002	0.0002	0.0020	0.0025	-	-	0.0021	0.0019
BOL	-	-	-	-	0.0001	-	-	-	-	-	0.0007	0.0023
BRA	-	0.0002	0.0005	0.0009	0.0001	0.0002	0.0012	0.0031	-	-	0.0017	0.0021
BFA	0.0000	-	0.0005	-	0.0002	-	0.0042	-	-	0.0001	0.0005	0.0010
CHL	0.0002	-	0.0005	-	0.0002	0.0003	0.0016	0.0025	-	-	0.0015	0.0029
CHN	0.0002	0.0002	-	-	-	0.0003	0.0011	0.0024	-	-	0.0010	0.0080
COL	-	-	-	-	-	0.0001	0.0009	0.0017	-	-	0.0009	0.0020
CRI	-	-	-	-	-	-	0.0007	-	-	-	0.0006	0.0021
CUB	-	-	0.0006	0.0012	0.0001	-	0.0014	-	-	-	0.0017	-
CYP	-	0.0003	-	-	0.0004	0.0002	0.0017	0.0040	0.0021	0.0003	0.0028	0.0030
ECU	-	-	0.0004	-	-	-	0.0010	0.0018	-	-	0.0012	0.0027
EGY	0.0001	0.0003	0.0006	-	0.0003	0.0003	0.0022	0.0029	0.0001	0.0003	0.0025	0.0016
SLV	-	-	-	-	0.0001	0.0001	0.0008	0.0011	-	-	0.0005	0.0015
HND	-	-	-	-	-	-	-	-	0.0001	-	-	-
HUN	-	0.0040	0.0014	-	0.0003	0.0005	0.0022	0.0116	0.0001	0.0003	0.0035	0.0018
IND	0.0003	-	0.0004	-	0.0002	0.0002	0.0011	0.0026	0.0000	-	0.0010	0.0024
JAM	-	-	-	-	-	0.0001	0.0008	-	-	0.0002	-	0.0027
MDG	0.0001	-	0.0006	-	0.0001	-	0.0057	0.0013	-	-	0.0007	0.0013
MYS	0.0008	-	-	-	-	0.0001	0.0009	0.0017	-	0.0003	0.0006	0.0083
MUS	0.0008	-	-	-	0.0002	-	0.0043	0.0019	0.0001	0.0002	0.0012	0.0021
MEX	-	-	-	-	-	-	-	-	-	-	-	-
NIC	-	-	0.0002	-	0.0002	0.0001	-	-	-	-	-	0.0020
PAN	-	-	-	-	0.0002	-	-	-	0.0001	-	-	0.0156
PRY	-	-	-	-	-	-	-	-	-	0.0001	0.0006	0.0020
PER	-	-	0.0004	-	0.0002	0.0001	0.0008	0.0017	-	-	0.0010	0.0026
PHL	0.0009	-	-	-	-	0.0002	0.0010	0.0017	-	0.0003	-	0.0090
ROM	-	0.0013	0.0010	-	0.0003	-	0.0031	0.0082	0.0007	-	0.0065	-
SGP	0.0005	-	-	-	-	0.0001	0.0010	0.0016	-	-	0.0007	0.0072
ZAF	0.0005	0.0003	0.0008	-	0.0002	0.0003	0.0015	0.0046	-	0.0003	0.0014	0.0026
SYR	-	0.0004	0.0010	-	0.0002	0.0002	0.0021	0.0031	0.0002	-	0.0029	0.0019
THA	0.0005	-	-	-	0.0002	0.0002	0.0009	0.0018	-	-	0.0006	0.0090
TTO	0.0002	-	-	0.0021	-	-	-	0.0018	-	0.0004	0.0009	0.0026
TUN	-	-	0.0010	-	-	0.0001	0.0049	0.0028	0.0001	-	0.0035	-
TUR	0.0001	0.0004	0.0009	-	0.0002	0.0003	0.0022	0.0050	0.0002	0.0002	0.0028	0.0014
UGA	-	0.0002	0.0006	0.0003	0.0003	-	0.0008	0.0014	0.0000	0.0002	0.0009	0.0018
URY	-	-	-	-	0.0001	-	0.0014	0.0016	0.0000	-	0.0017	0.0013
VEN	-	-	0.0004	-	-	0.0001	0.0008	0.0016	-	-	0.0013	0.0017

- denotes non significant (at the 5% threshold) while all figures are significant impact at the 5% level.

Table 8: Matrix of significant elasticities for OECD countries using trade flows ($W3$), Cont'd

	NLD	NZL	NOR	PRT	ESP	SWE	CHE	GBR	USA	BRA	CHN
AUS	-	0.0016	0.0001	-	0.0004	0.0010	0.0007	0.0033	0.0090	0.0003	0.0027
AUT	0.0016	-	-	0.0003	0.0007	0.0008	0.0016	0.0016	0.0023	-	-
BEL	0.0059	0.0000	-	0.0003	0.0008	0.0011	0.0006	0.0029	0.0028	0.0003	-
CAN	-	0.0001	-	-	-	0.0004	-	0.0014	0.0248	0.0003	-
DNK	0.0030	0.0001	0.0013	0.0005	0.0007	0.0048	0.0008	0.0035	0.0024	0.0002	0.0010
FIN	0.0018	-	0.0010	0.0004	0.0007	0.0048	0.0009	0.0032	0.0035	0.0002	0.0010
FRA	0.0021	-	0.0002	0.0005	0.0023	0.0007	0.0010	0.0031	0.0036	0.0002	0.0009
GER	0.0038	-	0.0003	0.0005	0.0014	0.0012	0.0020	0.0033	0.0040	0.0003	0.0014
GRC	0.0024	0.0001	0.0002	0.0002	0.0012	0.0007	0.0007	0.0024	-	0.0002	0.0007
IRL	0.0014	-	0.0002	0.0002	0.0006	0.0006	0.0004	0.0120	0.0057	-	-
ITA	0.0023	0.0000	0.0001	0.0002	0.0015	0.0007	0.0014	0.0025	0.0022	0.0003	0.0008
JPN	-	0.0003	0.0001	-	-	0.0006	0.0007	0.0016	0.0120	0.0005	0.0062
NLD	0.1791	-	0.0003	0.0003	0.0009	0.0012	0.0007	0.0038	0.0038	0.0004	0.0009
NZL	-	0.1786	0.0002	-	-	0.0008	0.0006	0.0027	0.0067	-	0.0019
NOR	0.0021	-	0.1787	0.0004	0.0008	0.0063	0.0007	0.0040	0.0035	-	0.0010
PRT	0.0015	-	0.0002	0.1786	0.0051	0.0004	0.0004	0.0019	-	0.0003	-
ESP	0.0015	-	0.0001	0.0009	0.1788	0.0006	0.0006	0.0027	0.0023	0.0002	0.0008
SWE	0.0028	-	0.0020	0.0004	0.0007	0.1789	0.0009	0.0042	0.0035	-	-
CHE	0.0024	-	-	0.0003	0.0008	0.0009	0.1788	0.0024	0.0032	0.0002	-
GBR	0.0032	0.0001	0.0005	0.0005	0.0012	0.0013	0.0008	0.1792	0.0054	0.0003	0.0009
USA	-	0.0001	0.0001	0.0001	0.0004	0.0006	0.0005	0.0020	0.1810	0.0007	0.0024
ARG	-	0.0000	-	-	0.0014	0.0004	0.0005	0.0009	0.0070	0.0068	0.0011
BOL	-	0.0000	-	-	0.0006	0.0006	-	-	0.0052	0.0057	-
BRA	0.0006	0.0000	-	0.0001	0.0006	0.0005	0.0006	0.0009	0.0071	0.1787	-
BFA	0.0005	-	-	-	0.0004	-	-	0.0005	0.0009	-	0.0004
CHL	-	0.0001	0.0001	0.0001	0.0013	0.0007	0.0004	0.0009	0.0084	0.0030	0.0014
CHN	-	0.0001	0.0001	-	0.0003	0.0005	0.0003	0.0007	0.0028	0.0003	0.1789
COL	-	-	-	-	0.0007	0.0003	0.0004	0.0007	0.0084	0.0010	-
CRI	0.0003	-	-	-	0.0005	-	0.0002	-	0.0118	0.0007	-
CUB	0.0006	0.0002	-	-	0.0045	-	0.0002	-	-	0.0006	0.0045
CYP	0.0008	0.0000	0.0005	0.0002	0.0010	0.0005	0.0004	0.0032	0.0033	0.0002	-
ECU	-	-	-	-	0.0009	-	0.0004	-	0.0083	0.0013	-
EGY	0.0007	0.0001	-	-	0.0006	0.0006	0.0006	0.0012	0.0028	0.0004	0.0005
SLV	-	0.0001	-	-	0.0004	-	0.0002	-	0.0082	0.0003	-
HND	0.0005	0.0000	-	-	0.0005	-	0.0003	-	0.0112	0.0004	-
HUN	0.0014	-	-	-	0.0007	0.0007	0.0010	0.0016	-	0.0003	0.0009
IND	0.0005	0.0001	0.0001	-	0.0002	0.0003	0.0007	0.0015	0.0029	0.0003	0.0007
JAM	0.0004	0.0002	-	-	0.0002	-	-	0.0015	0.0147	0.0006	-
MDG	0.0004	0.0000	-	-	0.0003	-	0.0002	0.0007	0.0010	0.0002	0.0009
MYS	-	0.0002	-	-	-	0.0003	0.0004	0.0012	0.0042	0.0002	0.0010
MUS	-	0.0003	-	0.0001	0.0003	-	0.0005	0.0020	-	0.0002	0.0016
MEX	-	0.0001	-	-	0.0004	-	-	-	0.0186	0.0004	-
NIC	0.0003	0.0001	0.0001	-	0.0006	-	0.0002	-	0.0069	0.0002	-
PAN	-	-	0.0003	-	0.0004	-	0.0003	-	0.0045	0.0004	-
PRY	-	-	-	-	0.0003	-	-	0.0008	0.0044	0.0076	-
PER	-	0.0003	-	-	0.0009	0.0004	0.0004	-	0.0080	0.0017	0.0010
PHL	0.0005	0.0002	-	-	-	0.0003	0.0003	0.0009	0.0054	0.0003	0.0013
ROM	0.0014	-	-	-	0.0005	0.0006	0.0009	0.0018	0.0018	0.0003	0.0006
SGP	0.0004	0.0001	0.0001	-	0.0002	0.0003	0.0003	0.0011	0.0044	0.0001	0.0011
ZAF	0.0009	0.0001	-	0.0001	0.0004	0.0004	0.0007	0.0030	0.0034	0.0003	0.0009
SYR	0.0008	0.0000	-	-	0.0006	0.0004	0.0003	0.0011	0.0014	0.0003	0.0008
THA	0.0004	0.0001	0.0001	-	-	0.0003	0.0004	0.0008	0.0040	0.0002	0.0014
TTO	0.0006	0.0002	0.0001	-	0.0004	-	-	0.0027	0.0153	0.0007	-
TUN	0.0006	0.0000	0.0000	0.0001	0.0008	0.0003	0.0003	-	0.0009	0.0001	-
TUR	0.0010	0.0000	0.0001	-	0.0008	0.0006	0.0007	0.0017	0.0023	0.0002	0.0006
UGA	0.0005	-	0.0001	-	0.0003	0.0002	0.0003	0.0027	0.0012	0.0002	0.0006
URY	-	0.0000	-	-	0.0011	0.0003	0.0004	0.0008	0.0038	0.0067	0.0007
VEN	0.0004	0.0001	-	-	0.0006	-	0.0003	0.0007	0.0098	0.0010	-

- denotes non significant (at the 5% threshold) while all figures are significant impacts at the 5% level.